# Appendix (Not for Publication) for: 

# Oil Price Shocks, Inventories and Macroeconomic Dynamics 

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#### Abstract

This paper investigates the time delay in the transmission of oil price shocks using disaggregated manufacturing data on inventories and sales. VAR estimates indicate that industry-level inventories and sales respond faster to an oil price shock than aggregate GDP, especially industries that are energy intensive. In response to an unexpected oil price increase, sales drop and inventories are accumulated. This leads to future reductions in production. We estimate a modified linear-quadratic inventory model to inquire whether the patterns observed in the VAR impulse responses are consistent with rational behavior by the firms. Estimation results suggest that three mechanisms play a role in the industry-level dynamics. First, oil prices act as a negative demand shock. Second, the shock catches manufacturers by surprise resulting in higher than anticipated inventories. Third, because of their desire to smooth production, manufacturers deviate from the target level of inventories and spread the decline in production over various quarters, hence the delay in the response of aggregate output.


Keywords: oil shocks, macroeconomic fluctuations, inventories.
JEL Classification: E22, E32,Q43.

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## 1 The Optimization Problem in Matrix Form

Note that, with constants set to zero, the cost function in (4) can be written as:

$$
C_{t}=(1 / 2) \mathbf{g}_{t}^{\prime} \mathbf{G}_{0} \mathbf{g}_{t}
$$

where $\mathbf{g}_{t}=\left[\begin{array}{c}Q_{t}-Q_{t-1} \\ Q_{t}-U_{c, t} \\ H_{t-1}-a_{3} S_{t}\end{array}\right]=\boldsymbol{\Lambda}^{\prime}\left[\begin{array}{c}u_{t} \\ \\ \mathbf{x}_{t}\end{array}\right]$.
Let $\boldsymbol{\Lambda}^{\prime}=\left[\begin{array}{cccccccc}1 & -2 & 1 & 0 & 0 & 0 & 1 & \mathbf{0}_{5} \\ 1 & -1 & 0 & 0 & -1 & 0 & 0 & \mathbf{0}_{5} \\ 0 & 1 & 0 & -a_{3} & 0 & 0 & -a_{3} & \mathbf{0}_{5}\end{array}\right]$,
$\mathbf{G}_{0}=\left[\begin{array}{ccc}a_{0} & 0 & 0 \\ 0 & a_{1} & 0 \\ 0 & 0 & a_{2}\end{array}\right]$,
and $\mathbf{x}_{t}=\left(H_{t-1}, H_{t-2}, S_{t-1}, v_{c, t}, v_{c, t-1}, v_{s, t}, v_{s, t-1}, o_{t}, o_{t-1}, o_{t-2}, o_{t-3}\right)^{\prime}$ denote the state vector that summarizes information relevant for the firm's decision, $u_{t}=H_{t}$ denote the control variable, and $\mathbf{0}_{5}$ denote a $(1 \times 5)$ vector of zeros.

Notice further that if we collect equations inventory identity(? ? ), the equation of motion for $\mathbf{x}_{t}$ (??) can be written as

$$
\begin{equation*}
\mathbf{x}_{t+1}=\mathbf{A} \mathbf{x}_{t}+\mathbf{B} u_{t}+\mathbf{C} \mathbf{w}_{t+1} \tag{1}
\end{equation*}
$$

$$
\begin{aligned}
& \text { where } \mathbf{A}=\left[\begin{array}{lllllllllll}
0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\
1 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\
0 & 0 & 1 & 0 & 0 & 1 & 0 & 0 & 0 & 0 & 0 \\
0 & 0 & 0 & \theta_{c 1} & \theta_{c 2} & 0 & 0 & 0 & 0 & 0 & 0 \\
0 & 0 & 0 & 1 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\
0 & 0 & 0 & 0 & 0 & \lambda_{s 1} & \lambda_{s 2} & \lambda_{o 1} & \lambda_{o 2} & \lambda_{o 3} & \lambda_{o 4} \\
0 & 0 & 0 & 0 & 0 & 1 & 0 & 0 & 0 & 0 & 0 \\
0 & 0 & 0 & 0 & 0 & 0 & 0 & \omega_{o 1} & \omega_{o 2} & 0 & 0 \\
0 & 0 & 0 & 0 & 0 & 0 & 0 & 1 & 0 & 0 & 0 \\
0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 1 & 0 & 0 \\
0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 1 & 0
\end{array}\right] ; \\
& \mathbf{B}=\left[\begin{array}{c}
1 \\
\mathbf{0}_{10}
\end{array}\right], \mathbf{0}_{10} \text { denotes a }(1 \times 10) \text { vector of zeros; } \\
& \mathbf{C}=\left[\begin{array}{lllllllllll}
0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\
0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\
0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\
0 & 0 & 0 & 1 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\
0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\
0 & 0 & 0 & 0 & 0 & 1 & 0 & \lambda_{o 0} & 0 & 0 & 0 \\
0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\
0 & 0 & 0 & 0 & 0 & 0 & 0 & 1 & 0 & 0 & 0 \\
0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\
0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\
0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0
\end{array}\right], \mathbf{w}_{t}=\left[\begin{array}{c}
0 \\
0 \\
\varepsilon_{s, t} \\
0 \\
0 \\
\varepsilon_{c, t} \\
\varepsilon_{o, t} \\
0 \\
0 \\
0
\end{array}\right]
\end{aligned}
$$

and all elements of $E\left(\mathbf{w}_{t} \mathbf{w}_{t}^{\prime}\right)$ are zero except the (4,4), (6,6), and (8,8), and elements, which are
$\sigma_{c c}, \sigma_{s s}$, and $\sigma_{o o}$, respectively.
Then the firm's optimization problem can then be rewritten as in equations (??) and (??):

$$
\min _{\left\{u_{t}\right\}_{t=0}^{\infty}} E\left\{\left.\sum_{t=0}^{\infty} \beta^{t}\left[\begin{array}{ll}
u_{t} & \mathbf{x}_{t}^{\prime}
\end{array}\right] \mathbf{G}\left[\begin{array}{c}
u_{t} \\
\mathbf{x}_{t}
\end{array}\right] \right\rvert\, \mathcal{F}_{0}\right\}
$$

subject to

$$
\mathbf{x}_{t+1}=\mathbf{A} \mathbf{x}_{t}+\mathbf{B} u_{t}+\mathbf{C} \mathbf{w}_{t+1}
$$

where $\mathcal{F}_{0}$ denotes the information set at $t=0$.

## References

[1] Elliott, Graham, Thomas J. Rothenberg, and James H. Stock (1996), "Efficient Tests for an Autoregressive Unit Root", Econometrica, 64, 813-836.
[2] Engle, Robert F. and Clive W.J. Granger (1987), "Cointegration and error correction: representation, estimation and testing," Econometrica, 55, 251-276.
[3] Perron, Pierre and Rodríguez, Gabriel (2003), "GLS Detrending, Efficient Unit Root Tests and Structural Change," Journal of Econometrics, 115(1), 1-27.
[4] Shea, John (1993), "The Input-Output Approach to Instrument Selection," Journal of Business and Economic Statistics, 11 (2), 145-155.

Table A.1. Time Series Properties of Manufacturing Inventories and Sales

| Sector | Unit root tests |  |  |  | Cointegration tests Inventories - Sales |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Inventories |  | Sales |  |  |  |
|  | ADF | DF-GLS | ADF | DF-GLS | EngleGranger | PerronRodriguez |
| Industries |  |  |  |  |  |  |
| Food | -1.614 | 1.147 | -0.940 | 2.270 | -3.165 * | -2.781 ** |
| Tobacco | -3.609 *** | -2.861 *** | -2.148 ** | -2.024 ** | -4.181 *** | -2.866 ** |
| Textiles | -2.050 | 1.249 | -1.599 | 0.616 | -3.181 * | -2.449 |
| Apparel | -2.407 | 0.874 | -2.028 | 0.505 | -6.782 *** | -6.063 *** |
| Paper | -2.151 | 2.517 | -2.259 * | 1.810 | -3.809 ** | -3.771 *** |
| Printing and publishing | -2.788 * | 2.025 | -2.055 | 1.397 | -2.977 | -2.971 ** |
| Petroleum products | -1.866 | 2.382 | -1.823 | 1.347 | -4.349 *** | -4.353 *** |
| Chemical | -2.809 * | -0.478 | -1.779 | 0.805 | -4.305 *** | -3.427 *** |
| Rubber and plastics | -1.188 | 2.073 | -1.016 | 1.626 | -3.722 ** | -3.427 *** |
| Leather | -2.851 * | -1.228 | -0.220 | 0.714 | -2.903 | -1.472 |
| Lumber | -3.611 *** | -0.156 | -1.435 | 0.485 | -5.041 *** | -2.914 ** |
| Furniture and fixtures | -1.673 | 2.275 | -0.558 | 1.470 | -2.927 | -2.021 |
| Stone, clay and glass products | -1.962 | 1.738 | -0.962 | 0.443 | -2.014 | -1.831 |
| Primary metals products | -2.464 * | -0.145 | -2.355 | -0.471 | -3.188* | -3.468 *** |
| Fabricated metals products | -1.356 | 2.480 | -1.409 | 1.093 | -3.040 | -2.997 ** |
| Industrial machinery | -0.955 | 2.650 | 1.279 | 3.565 | -1.510 | -0.943 |
| Electrical machinery | -1.969 | 2.217 | 0.589 | 3.217 | -2.612 | -1.014 |
| Transportation equipment |  |  |  |  |  |  |
| Motor vehicles | -0.859 | 1.131 | -1.616 | 0.431 | -5.143 *** | -5.260 *** |
| Other transportation equipment | -1.844 | 0.482 | -1.708 | -0.239 | -3.874 ** | -3.475 *** |
| Instruments | 0.595 | 3.471 | -1.827 | 2.653 | -1.097 | -0.396 |
| Other durables | -2.496 | 0.810 | -0.789 | 1.567 | -2.436 | -1.972 |
| Aggregates |  |  |  |  |  |  |
| Manufacturing | -2.297 | 2.492 | -0.476 | 2.132 | -4.868 *** | -2.989 ** |
| Nondurables | -2.358 | 2.141 | -1.688 | 1.912 | -4.370 *** | -3.883 *** |
| Durables | -1.092 | 3.282 | -0.120 | 2.099 | -2.581 | -2.212 |

Note: DF-GLS is the value for Elliott, Rothenberg and Stock (1996) unit root test; ADF is the value of the Augmented Dickey-Fuller test; Engle-Granger is the value of the Engle-Granger (1987) residual based cointegration test; Perron-Rodriguez is the value for Perron and Rodriguez (2001) residual based cointegration test. The number of lags for all tests was selected using the BIC. **, and * denote significance at the $1 \%, 5 \%$, and $10 \%$ level, respectively.

Table A. 2. Cost of Energy Input per Dollar of Output

|  | Cost of oil and natural gas <br> for each dollar of sale |
| :--- | :---: |
| Food | 0.027 |
| Tobacco | 0.009 |
| Textiles | 0.040 |
| Apparel | 0.030 |
| Paper | 0.035 |
| Printing and publishing | 0.012 |
| Petroleum products | 0.803 |
| Chemicals | 0.150 |
| Rubber and plastics | 0.036 |
| Leather | 0.031 |
| Lumber | 0.020 |
| Furniture and fixtures | 0.018 |
| Stone, clay, and glass products | 0.038 |
| Primary metals products | 0.044 |
| Fabricated metals products | 0.018 |
| Industrial machinery | 0.013 |
| Electrical machinery | 0.020 |
| Motor vehicles | 0.020 |
| Other transportation equipment | 0.012 |
| Instruments | 0.015 |

Note: computations based on the 1977 Input-Output tables published by the Bureau of Economic Analysis. This cost represents the total direct and indirect energy requirements per dollar of output sold by the particular industry.

Table A.3. Manufacturing Industries for which Motor vehicles Represent a Good Demand-shift Instrument

| SIC Industry | Instrument | DDS | UDS | DCS | UCS |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Three-digit SIC industries |  |  |  |  |  |
| 239 Miscellaneous apparel | Transportation equipment (SIC 37) | 30.6 | 18.5 | 2.3 | -- |
|  | Motor vehicles (SIC 371) | 29.2 | 17.2 | 3.2 | 1.6 |
| 253 Public building furniture | Transportation equipment (SIC 37) | 25.4 | 17.2 | -- | -- |
|  | Motor vehicles (SIC 371) | 23.2 | 14.9 | -- | -- |
| 301 Tires | Transportation equipment (SIC 37) | 19.1 | 13.0 | 4.3 | 2.1 |
| 304 Rubber and plastic hose and belting | Transportation equipment (SIC 37) <br> Motor vehicles (SIC 371) | 19.4 | 14.5 | 6.0 | 2.8 |
| 321,3229 Glass products, except containers | Transportation equipment (SIC 37) | 23.7 | 17.9 | 1.3 | 1.3 |
|  | Motor vehicles (SIC 371) | 21.5 | 15.2 | 1.7 | 1.5 |

[^1]Figure A. 1 a: Cumulative Response to a 10\% Increase in the Real Oil Price

Food


Paper




Tobacco


Printing and publishing



Textiles



Petroleum products


Apparel


NOTES: Estimates based on the reduced-form VAR(4) system described in section 3. 90\% confidence intervals computed using Kilian's (1998) bootstrap-after bootstrap method.

Figure A.1b: Cumulative Response to a $10 \%$ Increase in the Real Oil Price




Electrical machinery


$-0.002 \begin{array}{llllllllllll} & 2 & 2 & 4 & 6 & 8 & 10 & 12 & 14 & 16 & 18 & 20\end{array}$
Fabricated metal products





[^2]Figure A.1c: Cumulative Response to a 10\% Increase in the Real Oil Price


Other durable manufac.





NOTES: Estimates based on the reduced-form








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[^1]:    Source: Shea (1993).
    Notes:
    DDS: direct demand share of industry $I$ for industry $J$ is the share of domestically originating demand for $J$ 's output directly attributable to capital or intermediate purchases by industry $I$.
    UDS: ultimate demand share of industry $/$ for industry $J$ is the share of $J$ 's output ultimately embodied in final demand for $/$ incorporating both direct and indirect links.
    DCS: direct cost share of industry $Y$ for industry $Z$ is the value of $Y$ directly required as an intermediate or capital input per dollar of $Z$ 's output.
    UCS: ultimate cost share of industry $Y$ for industry $Z$ is the labor cost ultimately originating in $Y$ per dollar of $Z$ 's output.
    -- indicates unknown, less than $2 \%$.

[^2]:    NOTES: Estimates based on the reduced-form VAR(4) system described in section 3. 90\% confidence intervals computed using Kilian's (1998) bootstrap-after bootstrap method.

[^3]:    NOTES: Estimates based on the reduced-form VAR(4) system described in section 3. 90\% confidence intervals computed using Kilian's (1998) bootstrap-after bootstrap method.

