Due: Wednesday, March 6

1. Labor and capital are used to produce widgets according to the production table below:

|  | Labor Input |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Capital <br> Input |  | $\mathbf{1}$ | $\mathbf{2}$ | $\mathbf{3}$ | $\mathbf{4}$ | $\mathbf{5}$ |
|  | $\mathbf{1}$ | $\mathbf{2}$ | 40 | 40 | 55 | 65 |
|  | $\mathbf{3}$ | 55 | 60 | 75 | 85 | 90 |
|  | $\mathbf{4}$ | 65 | 75 | 90 | 100 | 105 |
|  | $\mathbf{5}$ | 75 | 90 | 100 | 110 | 115 |

a) Draw the $\mathrm{TP}_{\mathrm{L}}$ and the corresponding $\mathrm{AP}_{\mathrm{L}}$ and $\mathrm{MP}_{\mathrm{L}}$ curves when K is fixed at 2 in the short run.
b) Is this production process subject to the law of eventually diminishing marginal returns? Pick a set of combinations of inputs to illustrate and explain your answer.
c) Draw two points on the $\mathrm{Q}=40$ isoquant, four points on the $\mathrm{Q}=75$ isoquant, three points on the $\mathrm{Q}=90$ isoquant, and two points on the $\mathrm{Q}=115$ isoquant.
d) Calculate the $\mathrm{MRTS}_{\mathrm{L}, \mathrm{K}}$ along the $\mathrm{Q}=75$ isoquant. Show that it is diminishing.
e) Does this production exhibit increasing, constant, or decreasing returns to scale? Pick a set of combinations of inputs to illustrate and explain your answer. (Hint: start with $\mathrm{K}=1$ and $\mathrm{L}=1$, and then double all inputs. Then double all inputs again, and see what happens to Q.)
2. The production function for a firm that produces pizzas is $\mathrm{Q}=15 \mathrm{~K}^{1 / 4} \mathrm{~L}^{3 / 4}$. Q is the number of pizzas produced per hour, K is the number of pizza ovens, and L is the number of workers. In the short run K is fixed at 3 .
a) Write an equation for the firm's short-run production function showing output as a function of labor when K is equal to 3 .
b) Calculate total output per hour when $\mathrm{L}=0,1,2,3,4$, and 5 .
c) Calculate $\mathrm{MP}_{\mathrm{L}}$ for $\mathrm{L}=1$ to $\mathrm{L}=5$. Is $\mathrm{MP}_{\mathrm{L}}$ diminishing?
d) Calculate $\mathrm{AP}_{\mathrm{L}}$ for $\mathrm{L}=1$ to $\mathrm{L}=5$.
e) Graph $\mathrm{TP}_{\mathrm{L}}$. In a separate diagram, graph $\mathrm{AP}_{\mathrm{L}}$ and $\mathrm{MP}_{\mathrm{L}}$.
f) Does this firm experience decreasing, constant, or increasing returns to scale? Hint: set $\mathrm{K}=3$ and $\mathrm{L}=3$, and calculate Q . Then double both K and L , and show what happens to output.
3. Refer to Figure 7.3 in the text. Calculate and graph $\mathrm{TP}_{\mathrm{L}}, \mathrm{AP}_{\mathrm{L}}$, and $\mathrm{MP}_{\mathrm{L}}$ when K is fixed at $\mathrm{K}=3$.

