

1. See answer key to Question # 3, Test #1, Fall 2003.
2. See answer key to Question #5, Final Exam, Fall 2003.
3. See answer key to Question # 5, Test #1, Fall 2003.

4. $U = X^{.3} Y^{.7}$

$$X^* = .3 I / P_x \quad Y^* = .7 I / P_y$$

(a) $U = (.3 I / P_x)^{.3} (.7 I / P_y)^{.7} = .54 I P_x^{-.3} P_y^{-.7}$

$$E = 1.84 U P_x^{.3} P_y^{.7}$$

(b) $X_c = \frac{dE}{dP_x} = .55 U P_x^{-.7} P_y^{.7}$

(c) Slutsky eq: $\frac{dX}{dP_x} = \frac{dX}{dP_x} \Big|_{\bar{u}} - X \frac{dX}{dI}$

Marshallian: $\frac{dX}{dP_x} = -.3 I / P_x^2 \quad \checkmark$

substitution effect: $\frac{dX}{dP_x} \Big|_{\bar{u}} = \frac{dX_c}{dP_x}$

$$\frac{dX_c}{dP_x} = -.385 U P_x^{-1.7} P_y^{.7}$$

but $U = .54 I P_x^{-.3} P_y^{-.7}$

$$\text{so } \frac{dX_c}{dP_x} = -.21 I P_x^{-2}$$

income effect: $-X \frac{dX}{dI} = -(.3 I P_x^{-1}) (.3 P_x^{-1})$

$$= -.09 I P_x^{-2}$$

subst. effect + income effect = $-.21 I P_x^{-2} - .09 I P_x^{-2}$

$$= -.3 I / P_x^2 \quad \checkmark$$

so Slutsky equation checks out!